

Working at the limit

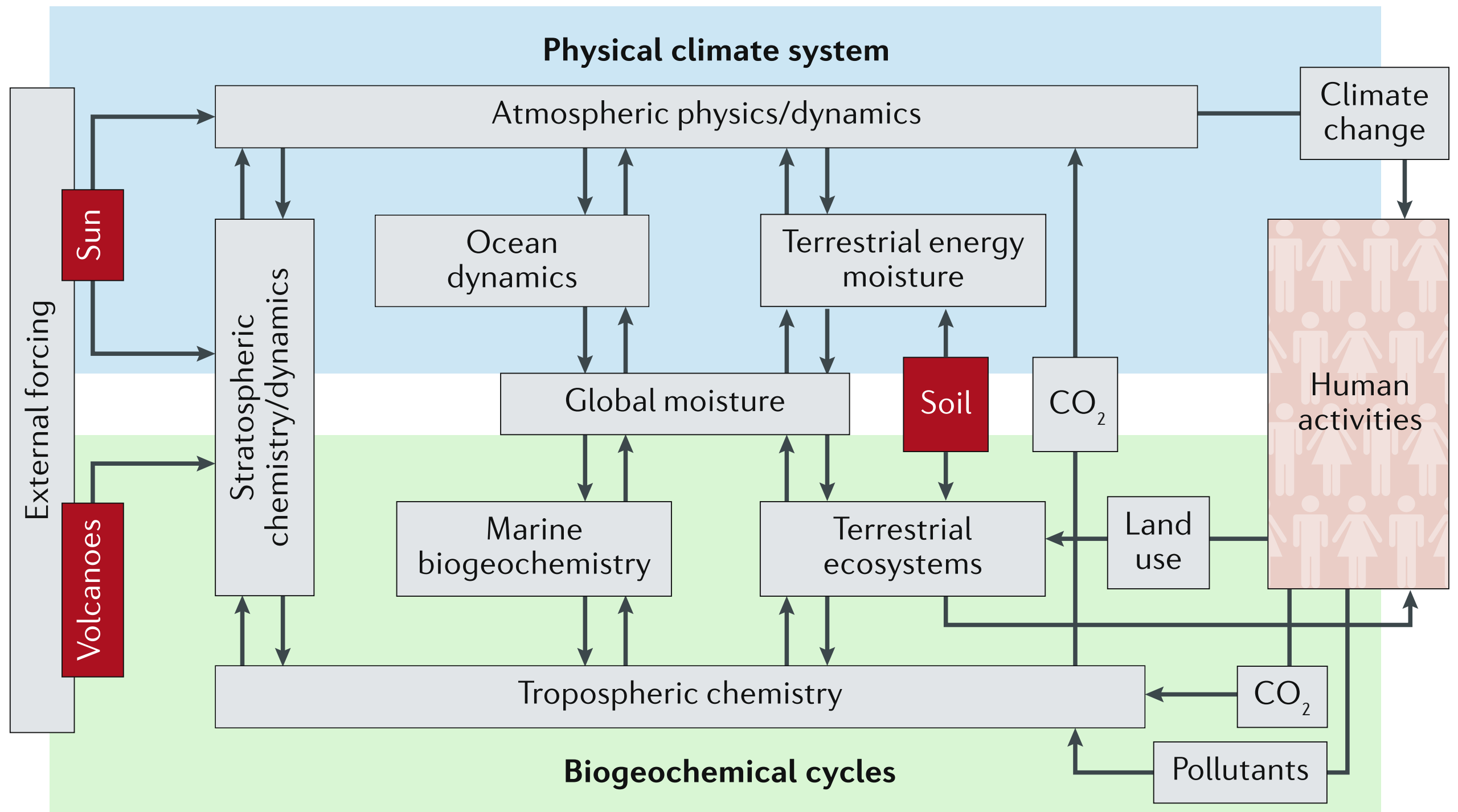
How thermodynamics shapes the Earth system



India Tour
April 2023

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The “Bretherton Diagram” of Earth System Science

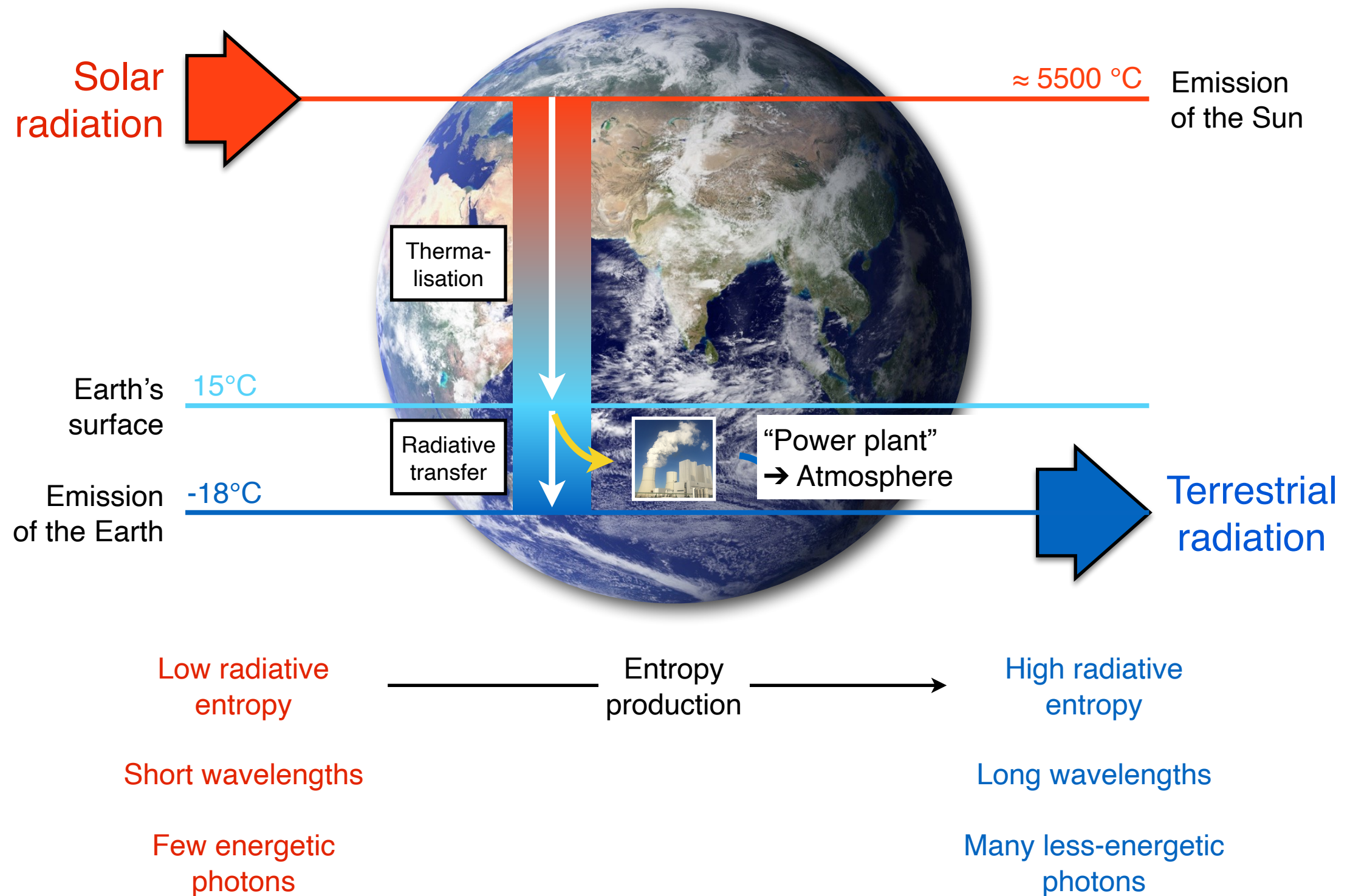


Why do things happen on Earth?



- Entropy and the “Second Law”
- Direction for the Earth system
- Sets limits for energy conversions
- Constrains *work* to run dynamics
- *Working at the limit*
- Climate, hydrology, vegetation
- Basis for Earth system science,
(renewable energy, sustainability,
planetary evolution)

Thermodynamics of the Planet



Setting Limits to Free Energy



First law: Energy conservation

$$J_{in} = J_{out} + G$$

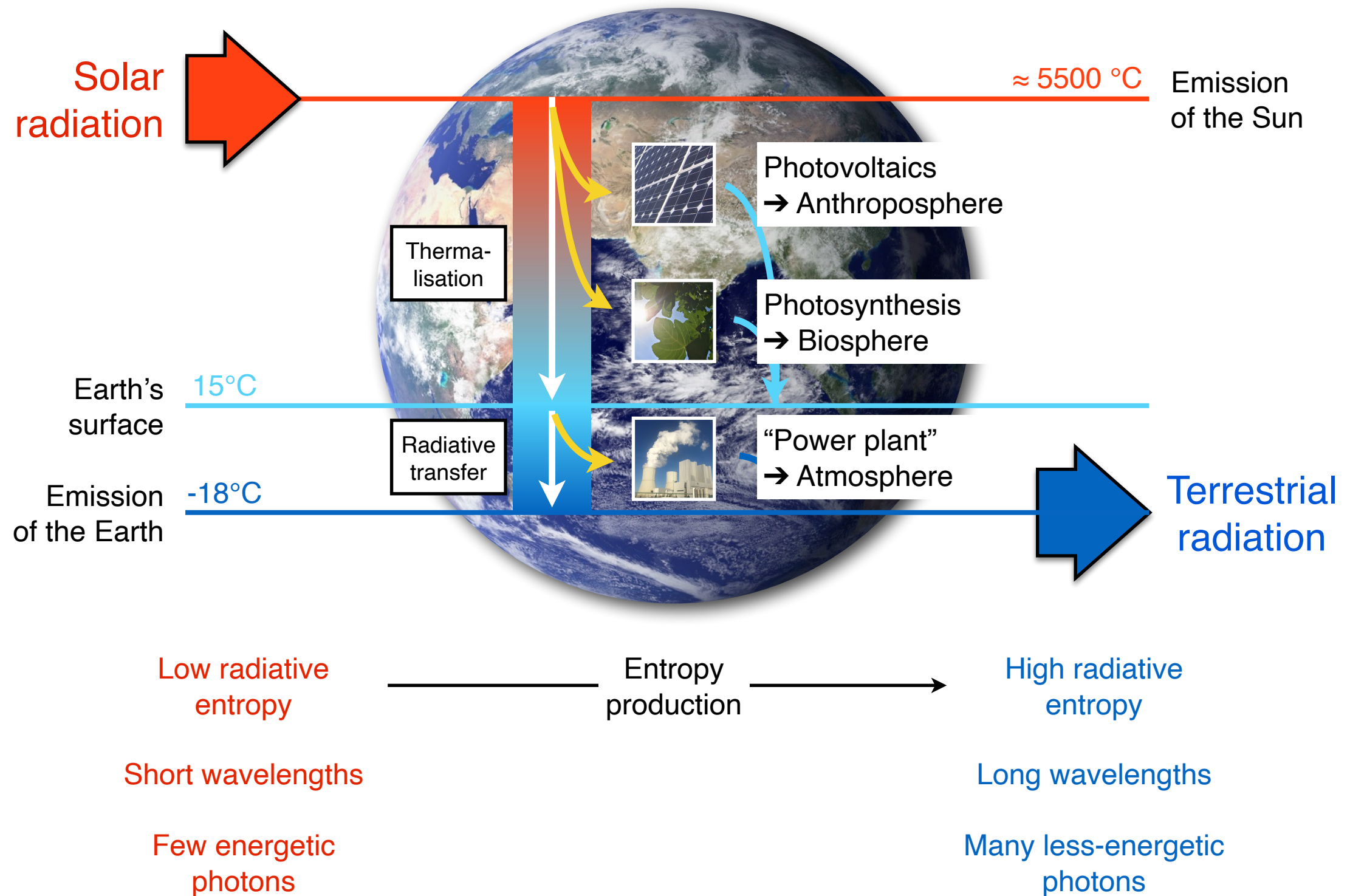
Second law: Entropy increase

$$\frac{J_{out}}{T_{out}} = \frac{J_{in}}{T_{in}} + \sigma$$

Free energy
(no entropy)

$$G \leq J_{in} \cdot \frac{T_{in} - T_{out}}{T_{in}}$$

Thermodynamics of the Planet





Outline

1. Powering climate

How thermodynamics constrains motion and determines temperatures

2. Powering cycling

How thermodynamics shapes evaporation and hydrologic cycling

3. Powering life

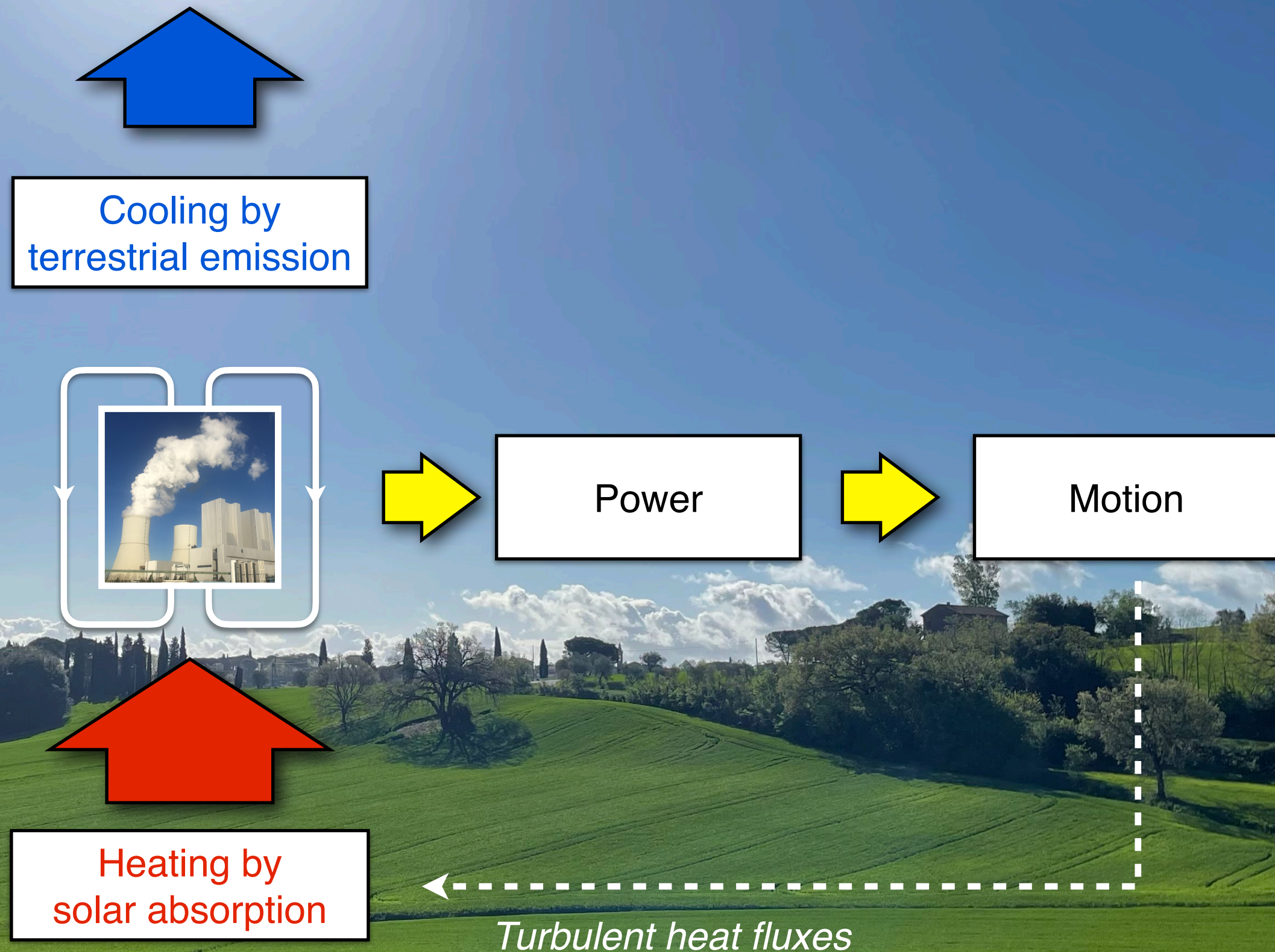
How thermodynamics constrains photosynthesis indirectly and how vegetation can push its limits

4. Powering human societies

Energy and future sustainability

5. Summary

Powering Climate



Working at the Limit

Radiative
Cooling
(high entropy)

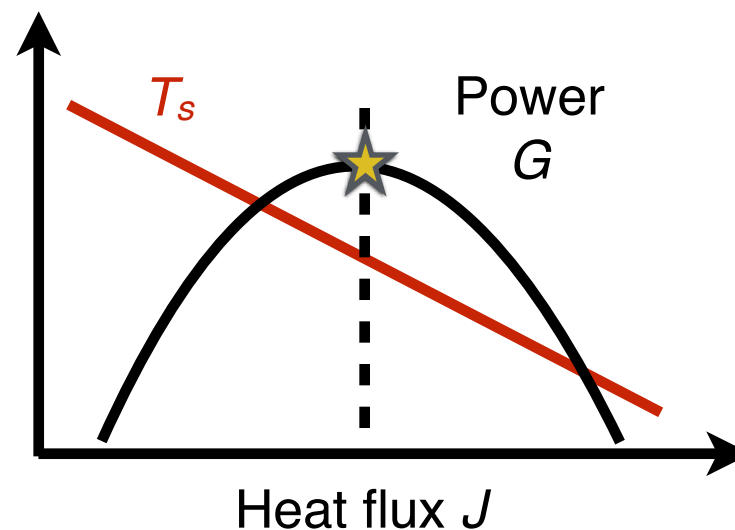


Radiative
Heating
(low entropy)

Thermodynamic limit:

$$G = J \cdot \frac{T_s - T_r}{T_s}$$

Maximum power limit:



Top-of-atmosphere budget:

$$R_{l,toa} = \sigma T_r^4 \approx \overline{R_{s,tot}}$$

$$T_s - T_r \approx \frac{R_s - R_{l,0} - J}{k_r}$$

Surface energy budget:

$$R_s + R_{l,d} = \sigma T_s^4 + J$$

For simplicity: $J = H + LE$

Working at the Limit

Radiative
Cooling
(high entropy)



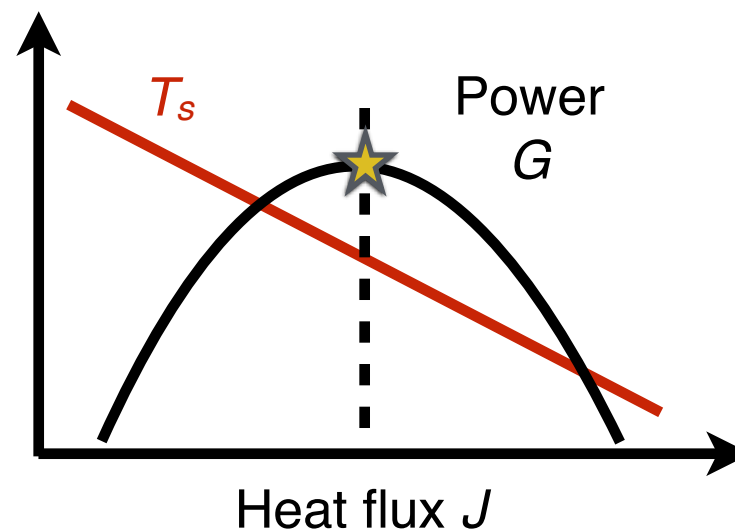
Radiative
Heating
(low entropy)



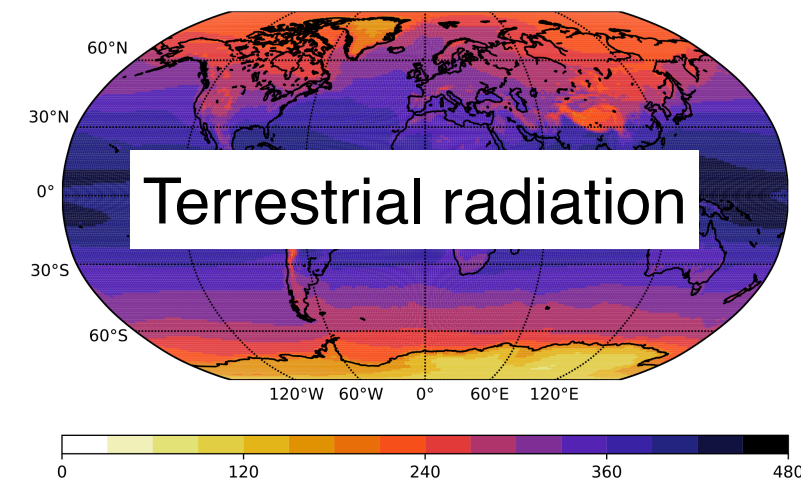
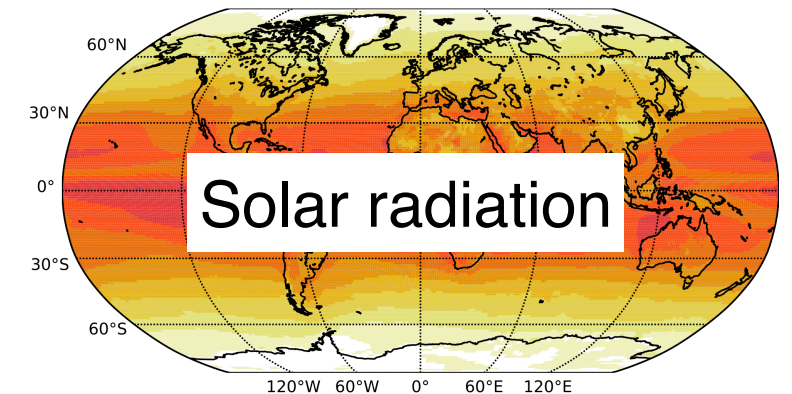
Thermodynamic limit:

$$G = J \cdot \frac{T_s - T_r}{T_s}$$

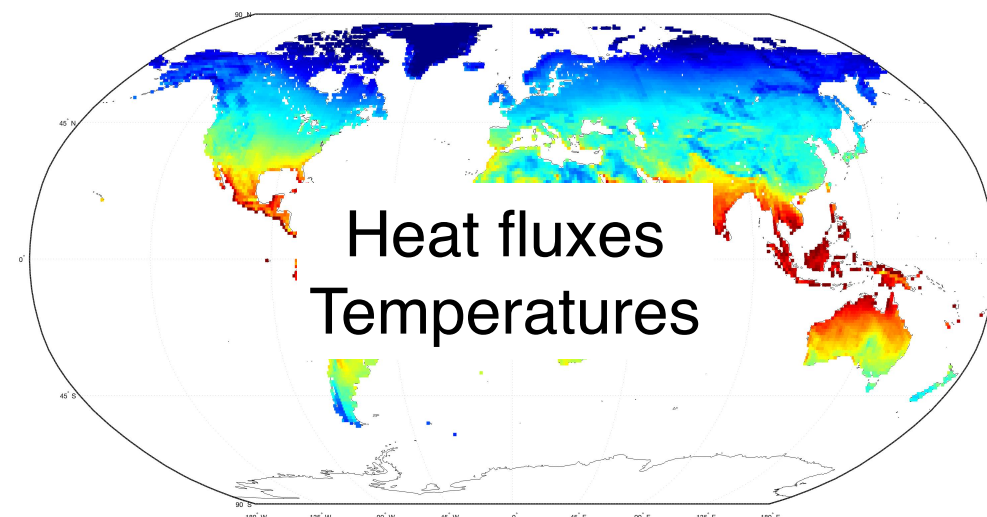
Maximum power limit:



NASA-CERES datasets



↓ Max. power



Working at the Limit

Radiative
Cooling
(high entropy)



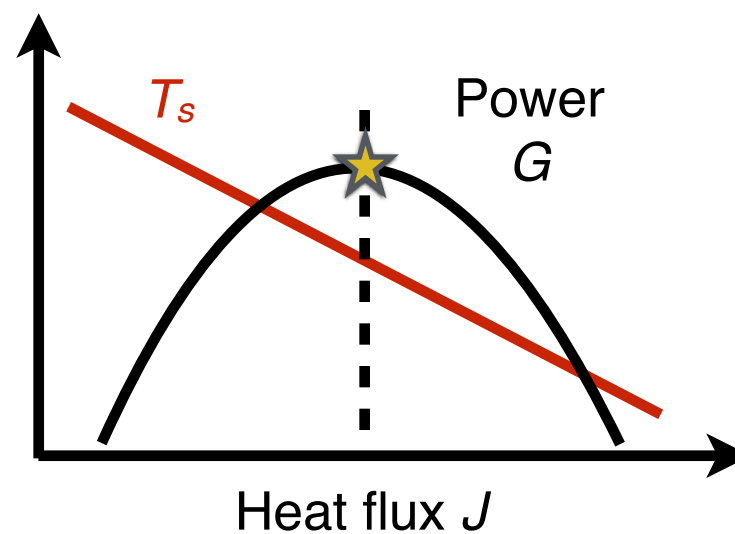
Radiative
Heating
(low entropy)



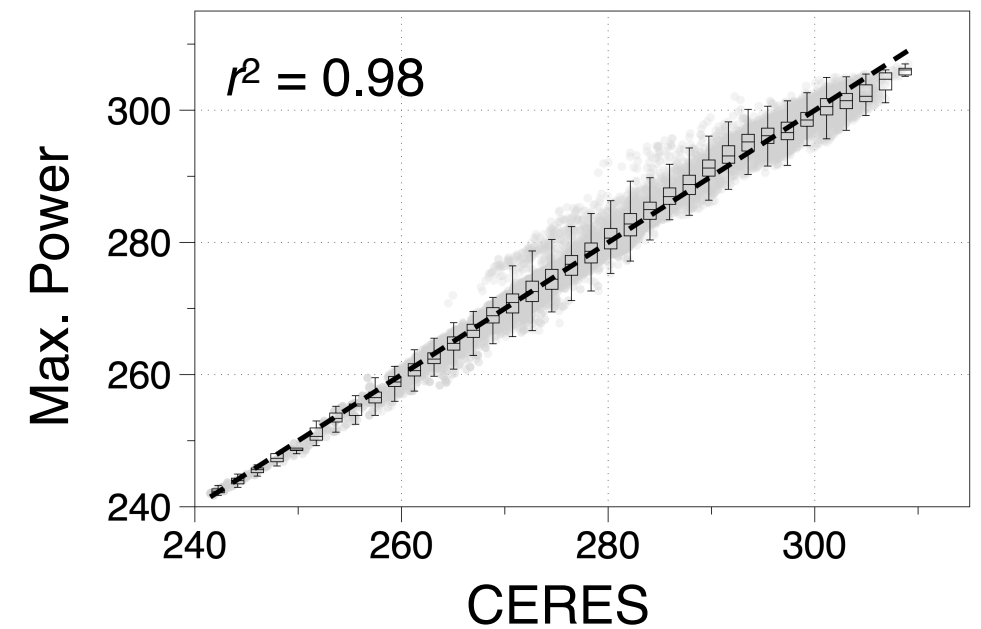
Thermodynamic limit:

$$G = J \cdot \frac{T_s - T_r}{T_s}$$

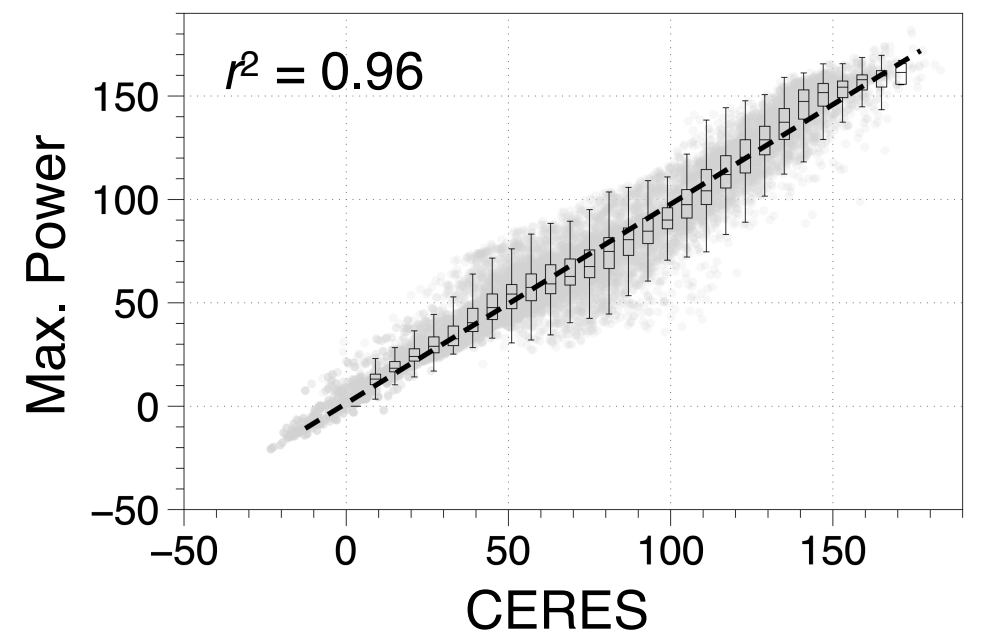
Maximum power limit:



Surface temperatures T_s

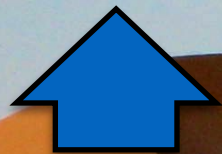


Heat fluxes J

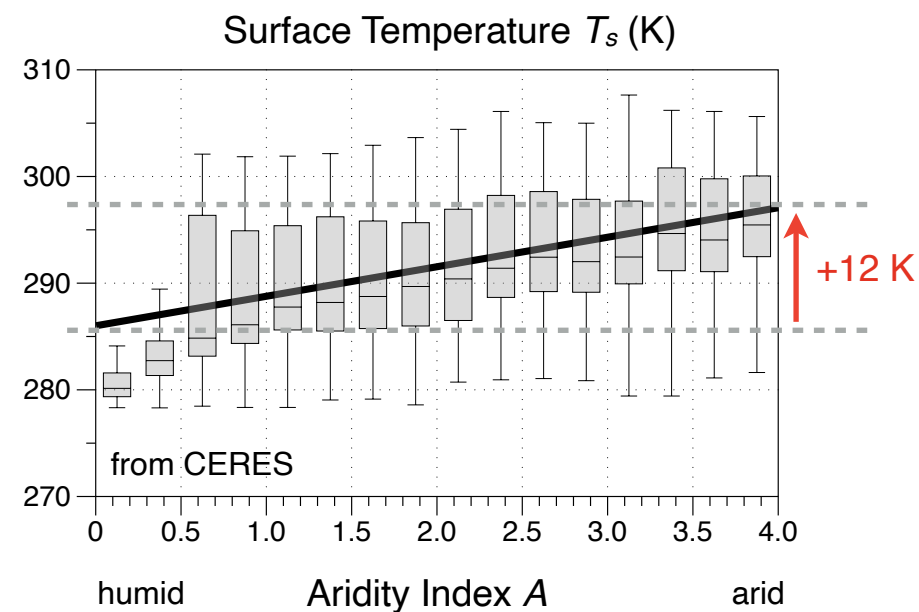


Working at the Limit

Radiative
Cooling
(high entropy)



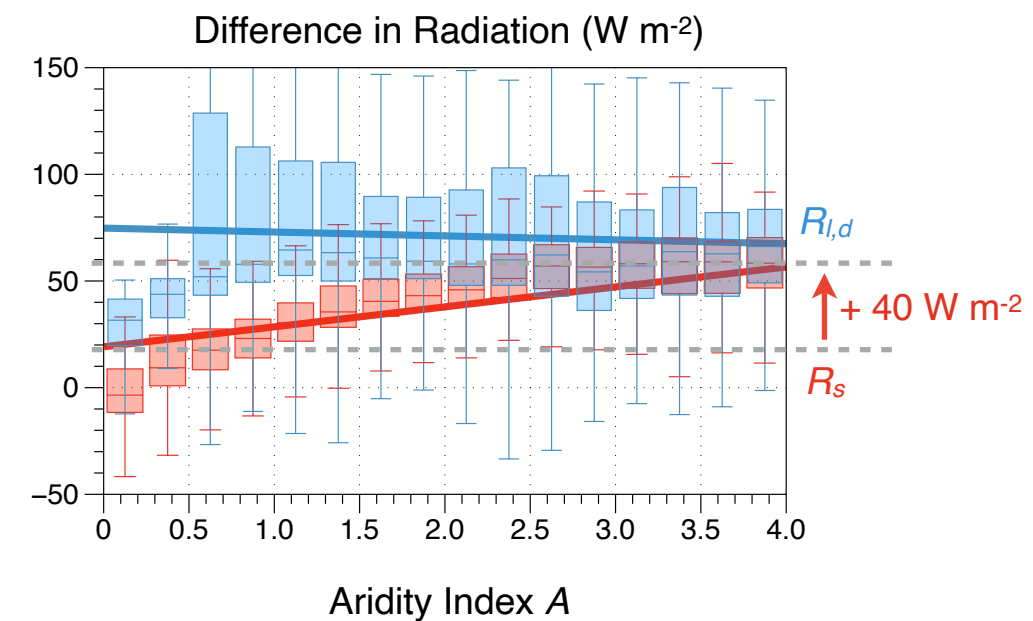
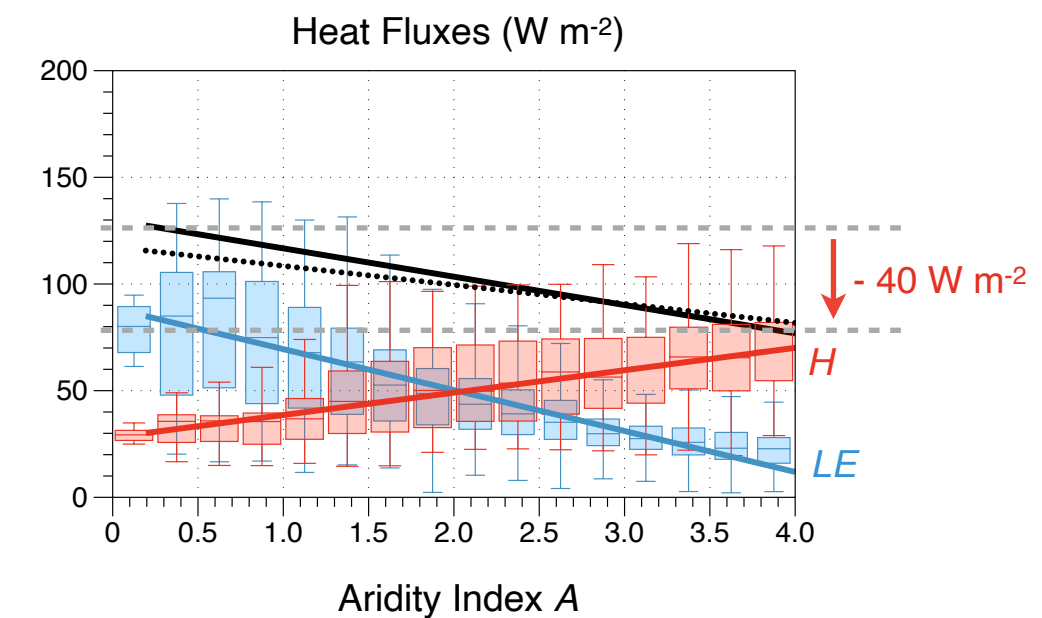
Radiative
Heating
(low entropy)



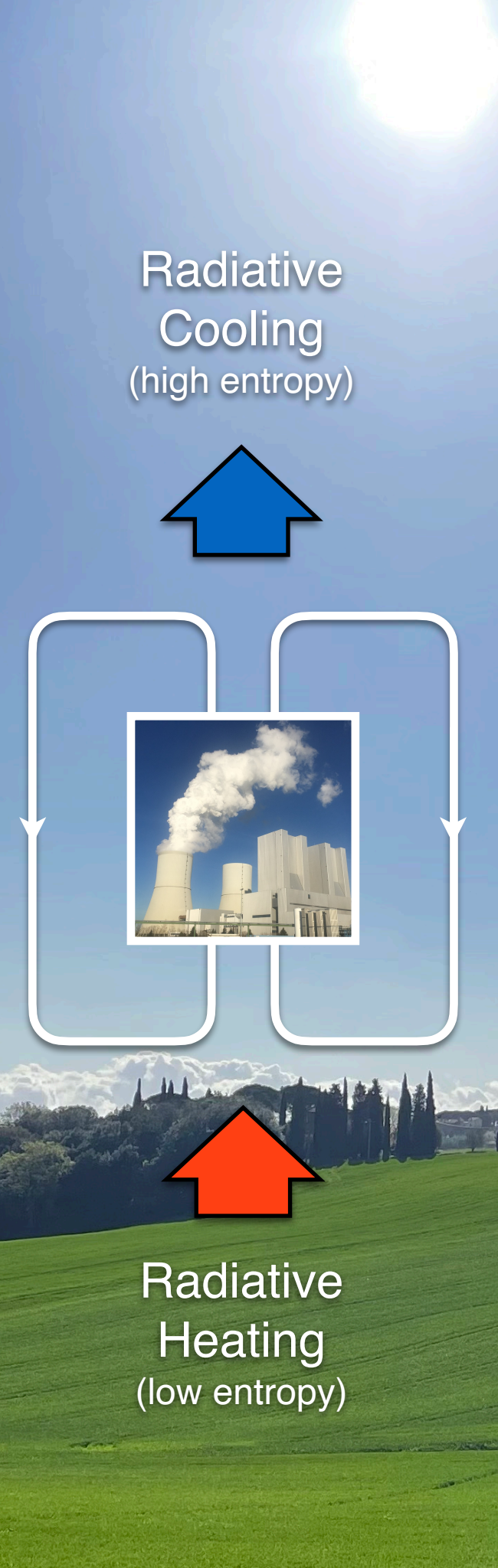
$$\Delta T_s = \frac{\Delta R_s + \Delta R_{l,d} - \Delta LE - \Delta H}{4\sigma T_{s,0}^3}$$

$$\Delta T_s \approx +14 \text{ K}$$

mostly because of less clouds
and less efficient heat engine



Powering Climate



- **Disequilibrium:** Spatiotemporal separation of absorption of solar radiation and emission to space
- **Heat engine:** Generates convective motion and turbulent heat fluxes; depletes disequilibrium
- **Working at the limit:** Heat fluxes deplete temperature difference, resulting in a maximum in power
- **Application:** Deserts are warmer because of less clouds and less efficient heat engine
- **Implication:** Surface temperatures are directly (and indirectly) mostly determined by radiation

Powering Cycling

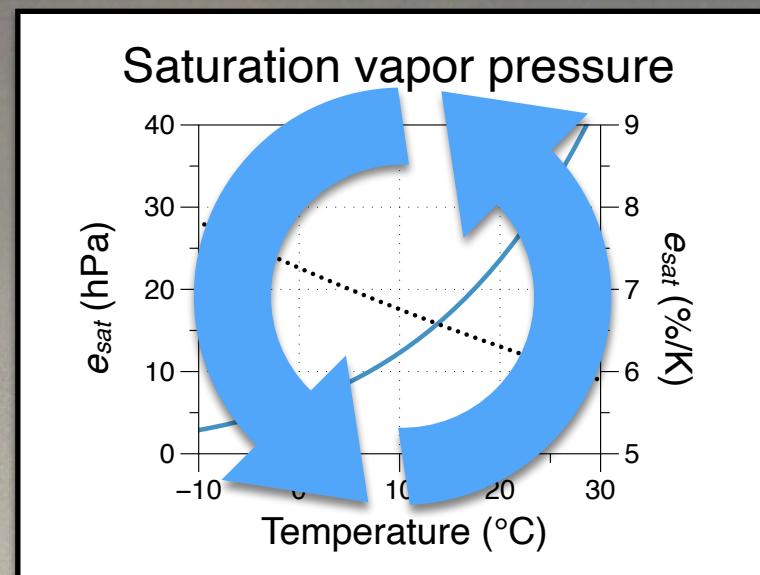
Condensational
Heating
(high entropy)



Equilibrium at
cold temperature
favours liquid
or ice

Liquid ← Condensation — Vapor

Precipitation



Buoyant
transport

Liquid — Evaporation → Vapor

Equilibrium at
warm temperature
favours vapor

Evaporative
Cooling
(low entropy)



Latent heat flux
 LE

Partitioning of Surface Heating

Heating of air

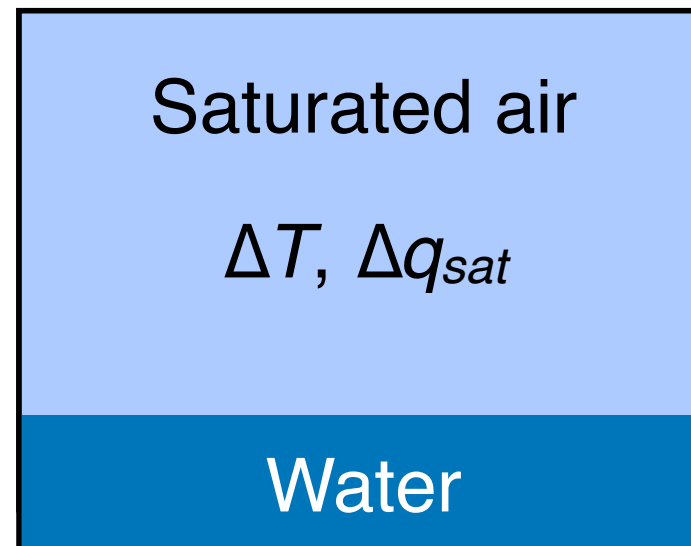
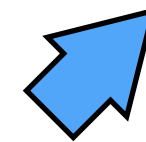
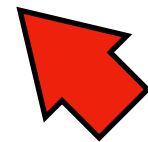
Increase in
thermal energy

$$\Delta U_{th} = c_p \rho V \cdot \Delta T$$

Moistening of air

Increase in
latent heat

$$\Delta U_{le} = L \rho V \cdot \Delta q_{sat}$$



Energy added:
 ΔU

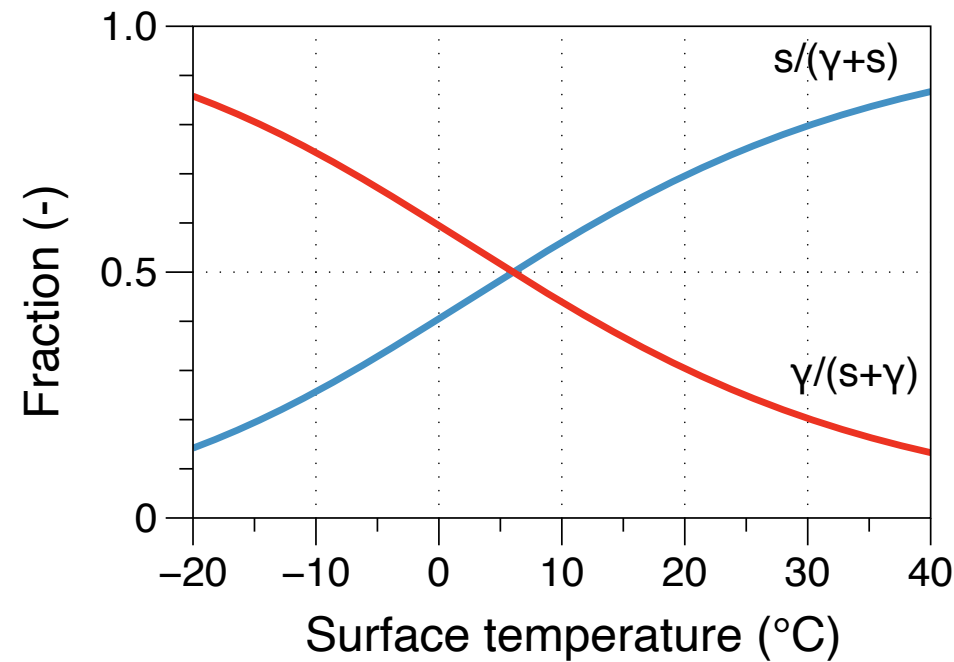
“Equilibrium
partitioning” of
turbulent fluxes
at the surface
(Schmidt, 1915)

Heating of air

Increase in
thermal energy

$$\Delta U_{th} = \frac{\gamma}{\gamma + s} \cdot \Delta U$$

Sensible
Heat Flux



Moistening of air

Increase in
latent heat

$$\Delta U_{le} = \frac{s}{\gamma + s} \cdot \Delta U$$

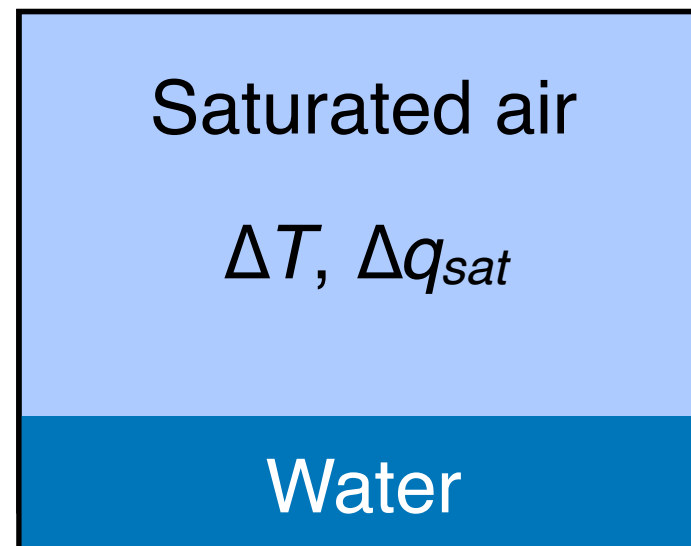
γ : psychrometric constant
 s : slope of saturation
 vapour pressure, de_{sat}/dT
 ("Clausius-Clapeyron")

Latent
Heat Flux

Equilibrium
Evaporation

or

Potential
Evaporation



Energy added:
 ΔU

Working at the limit

Condensational
Heating
(high entropy)



Liquid ← Vapor

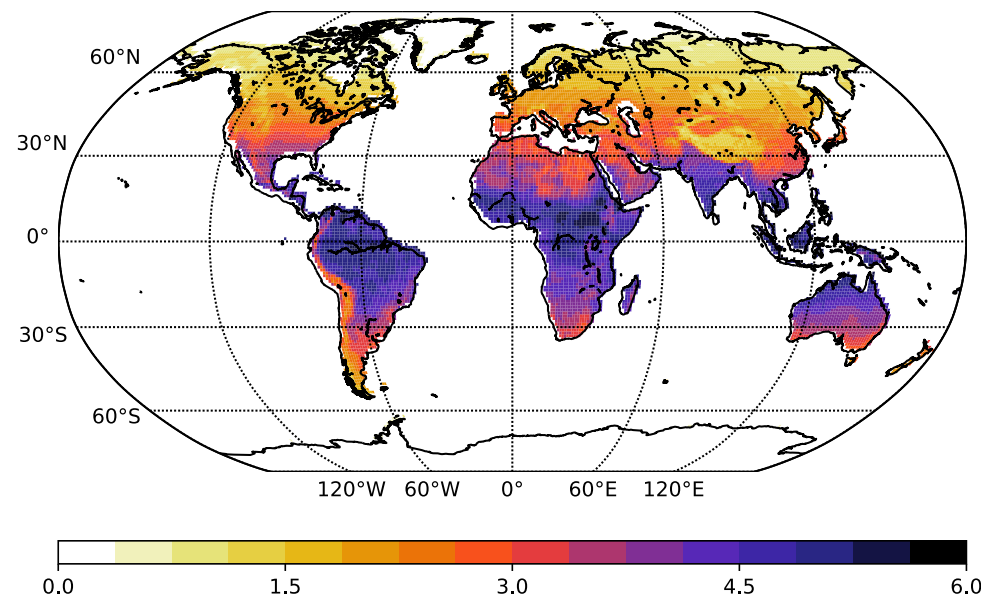


Liquid → Vapor

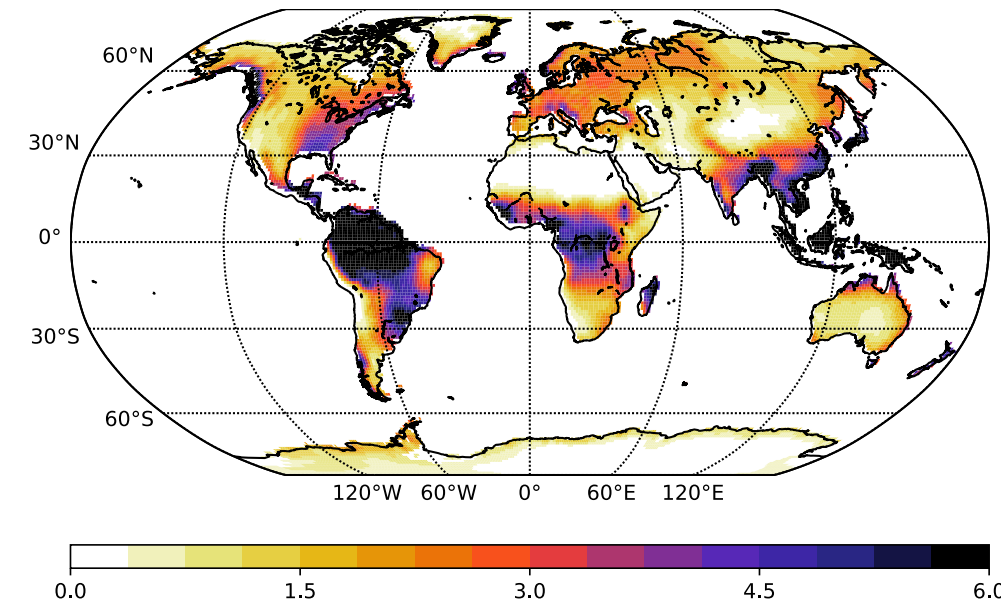


Evaporative
Cooling
(low entropy)

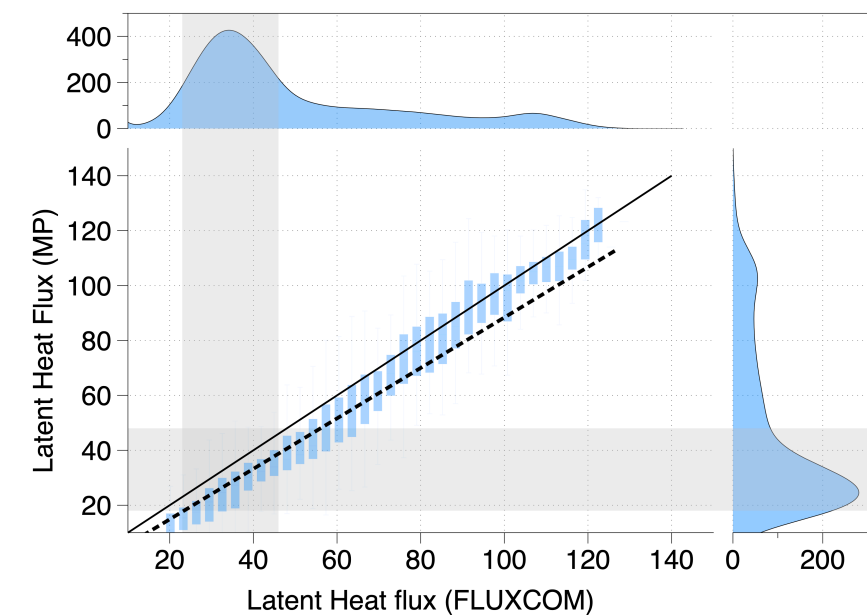
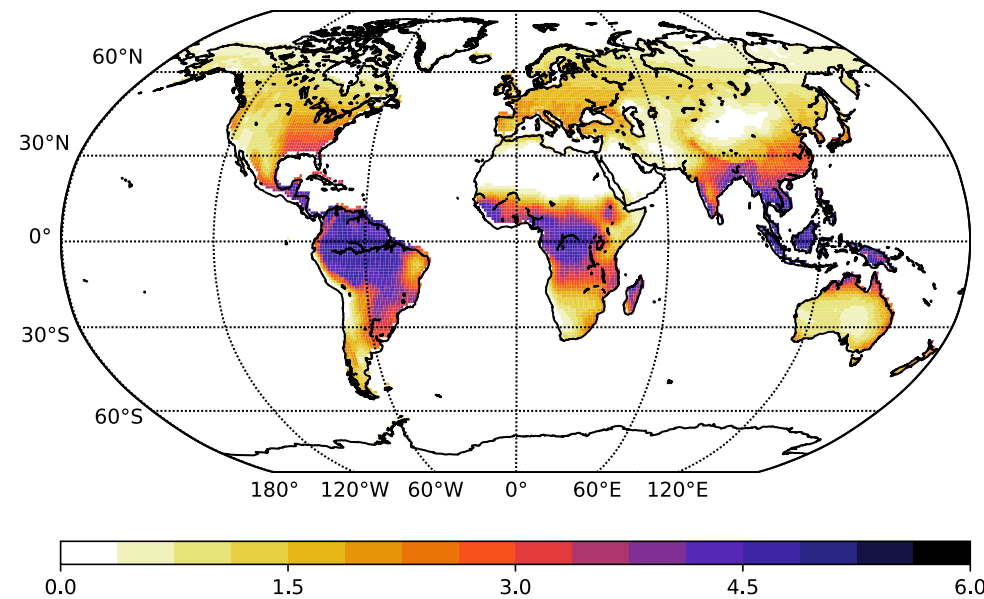
Potential Evaporation (mm d⁻¹)



Precipitation (mm d⁻¹)



Actual Evaporation (mm d⁻¹)



Hydrologic Cycling and Global Change

Condensational
Heating
(high entropy)



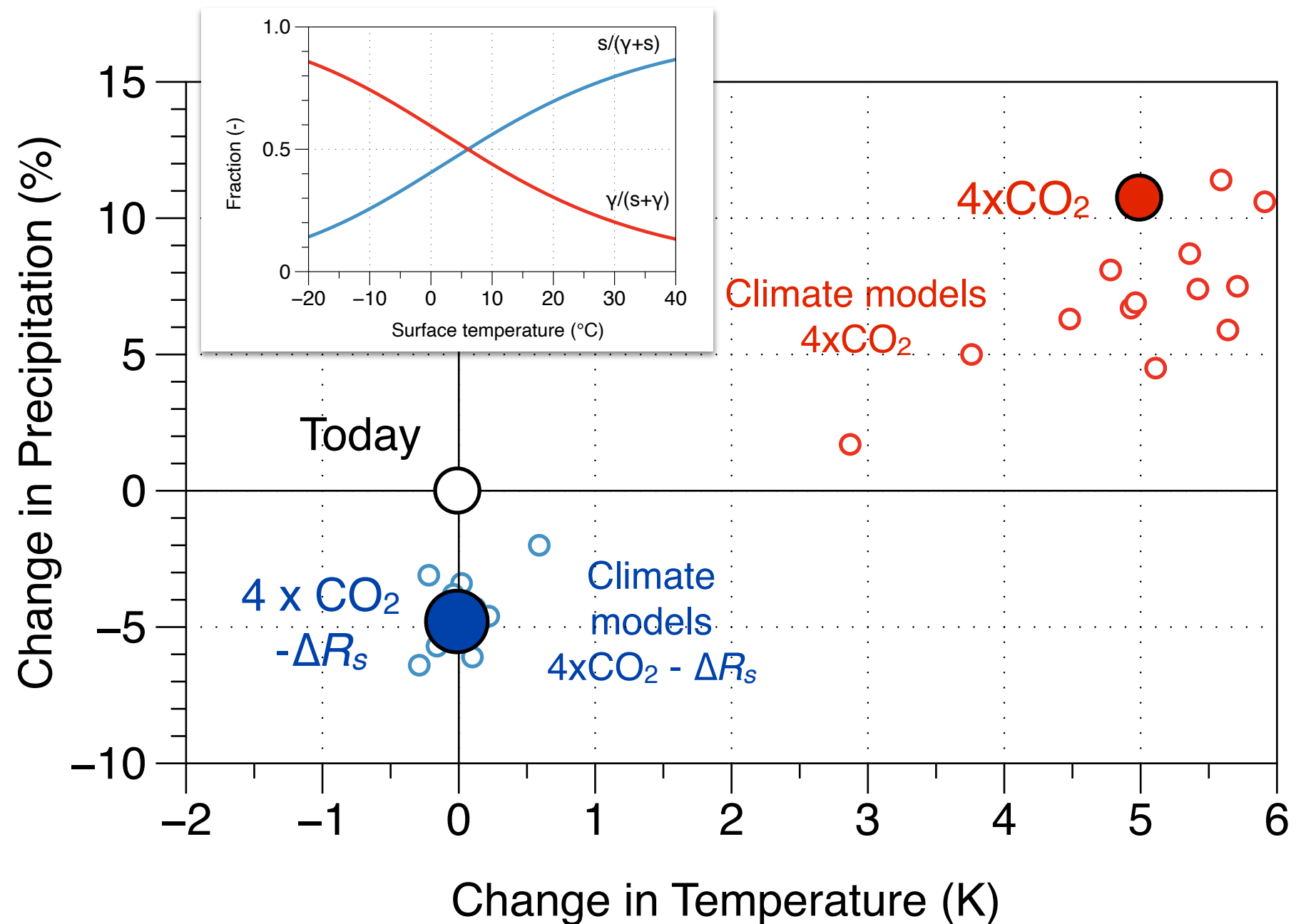
Liquid ← Vapor



Liquid → Vapor



Evaporative
Cooling
(low entropy)



Powering Cycling

Condensational
Heating
(high entropy)



Liquid ← Vapor



Liquid → Vapor



Evaporative
Cooling
(low entropy)

- **Disequilibrium:** Spatiotemporal separation of evaporation and condensation
 - Generated by dehumidification by precipitation
 - Depletion by evaporation
 - Requires vertical motion to operate
- **Working at the limit:** Indirect constraint by equilibrium partitioning combined with max. power heat fluxes
- **Application:** Sensitivity of hydrologic cycle to global warming reflects mostly the shift in equilibrium partitioning
- **Implication:** Rate of hydrologic cycling is set by thermodynamics

Powering Life

Dissipative Heating
(high entropy)

Chemical
equilibrium

Chemical
disequilibrium

Biosphere

Metabolism

Photosynthesis

Calvin cycle

$\uparrow \text{H}^+ + \text{e}^-$

Photosystems

Organic
carbon
 CH_2O

Oxygen
 O_2

Chemical
Free Energy

Solar radiation
(low entropy)

Water
 H_2O

Carbon
dioxide
 CO_2

Thermodynamic Efficiency of Photosynthesis

Solar
Radiation
(low entropy)



$\text{CH}_2\text{O}, \text{O}_2 \leftarrow \text{H}_2\text{O}, \text{CO}_2$



$\text{CH}_2\text{O}, \text{O}_2 \rightarrow \text{H}_2\text{O}, \text{CO}_2$



Dissipative
Heating
(high entropy)

8 - 10 photons of 1.8 eV
14.4 - 18 eV
Compare to 13.6 eV for $\text{H}^+ + \text{e}^-$

1.4 MJ/mol C



Photosynthesis

0.48 MJ/mol C

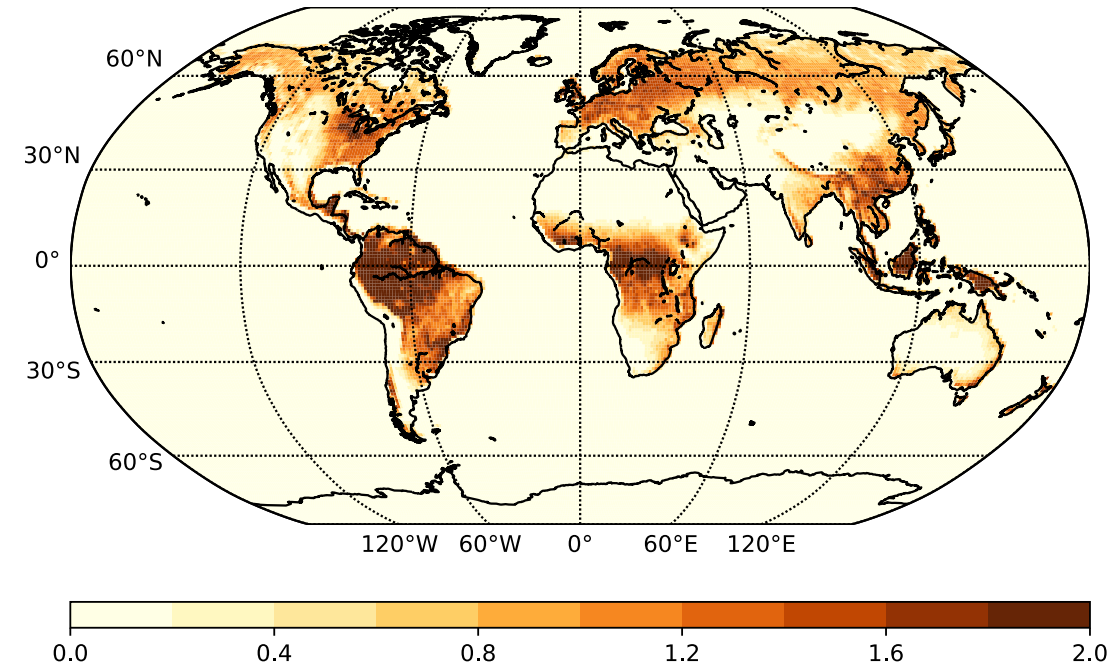


Glucose

Efficiency

$$0.48/1.4 \times 55\% \approx 17\%$$

Duysens (1962)
Radmer & Kok (1977)
Landsberg and Tonge (1980)
Hill and Rich (1983), ...



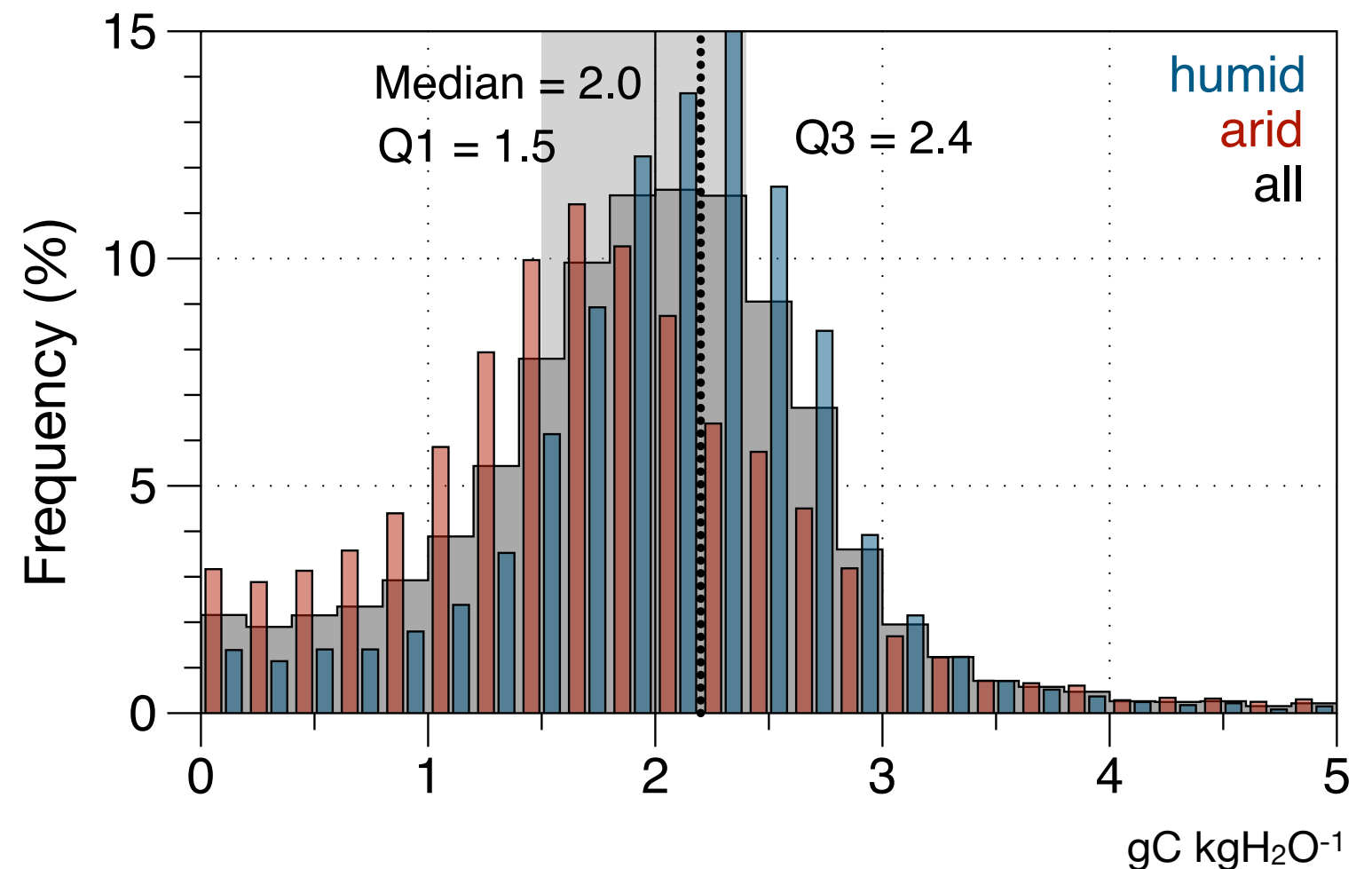
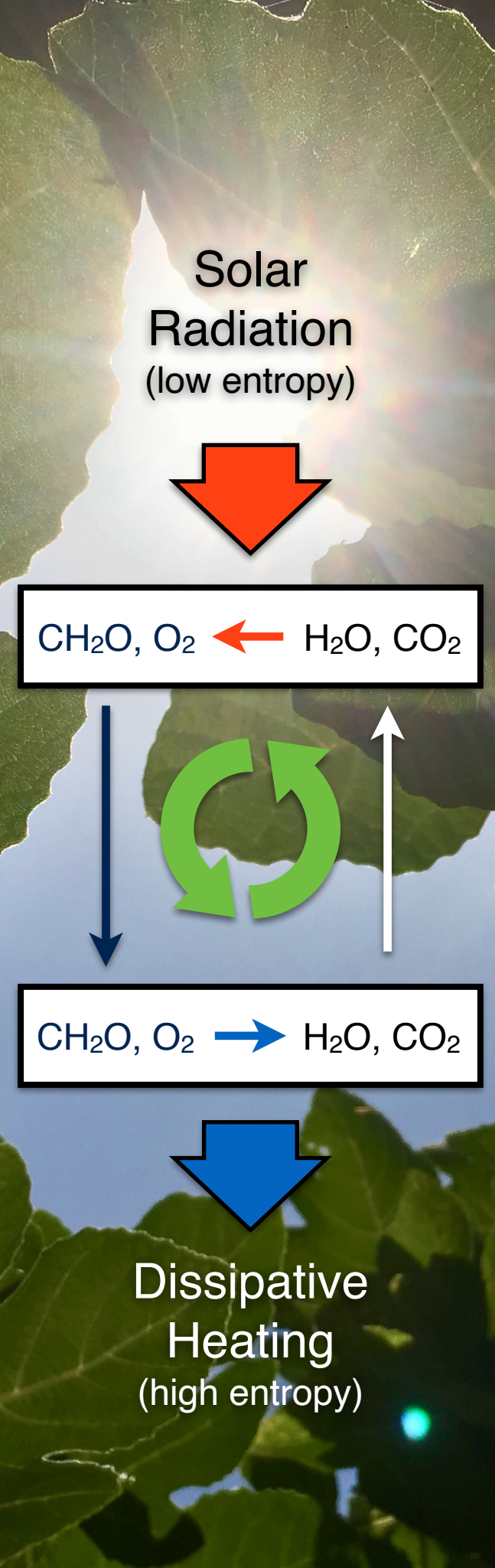
Data: NASA-CERES; CASA-GFED

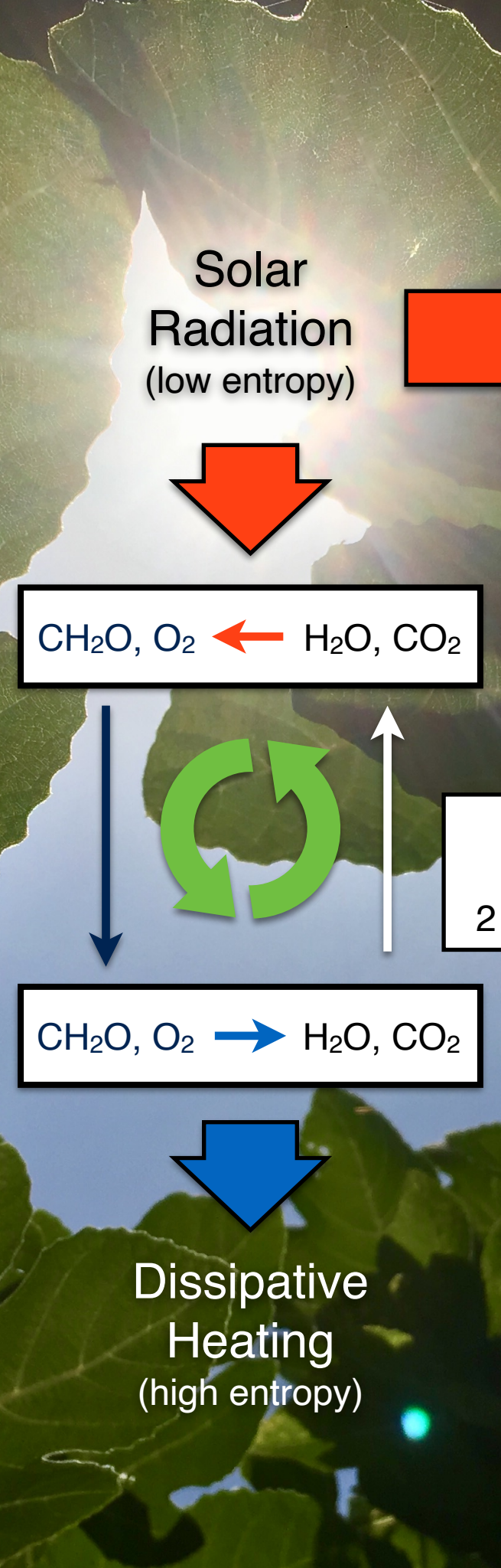
Efficiency

$$\approx 1-2\%$$

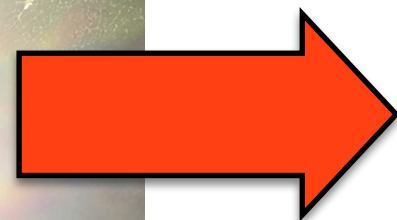
Kleidon (2021) BBA Bioenergetics

Water Use Efficiency





Solar
Radiation
(low entropy)



Radiative
heating

Maximum
power
 $\approx 50\%$



Turbulent
fluxes



Equilibrium
Evaporation

Equilibrium
partitioning
 $s/(s + \gamma) \approx 70\%$

Photosynthetic
efficiency:

$50\% \times 70\% \times 3.6\%$

$\approx 1.2\%$

$\text{CH}_2\text{O}, \text{O}_2 \leftarrow \text{H}_2\text{O}, \text{CO}_2$

Gas
exchange

H_2O



CO_2

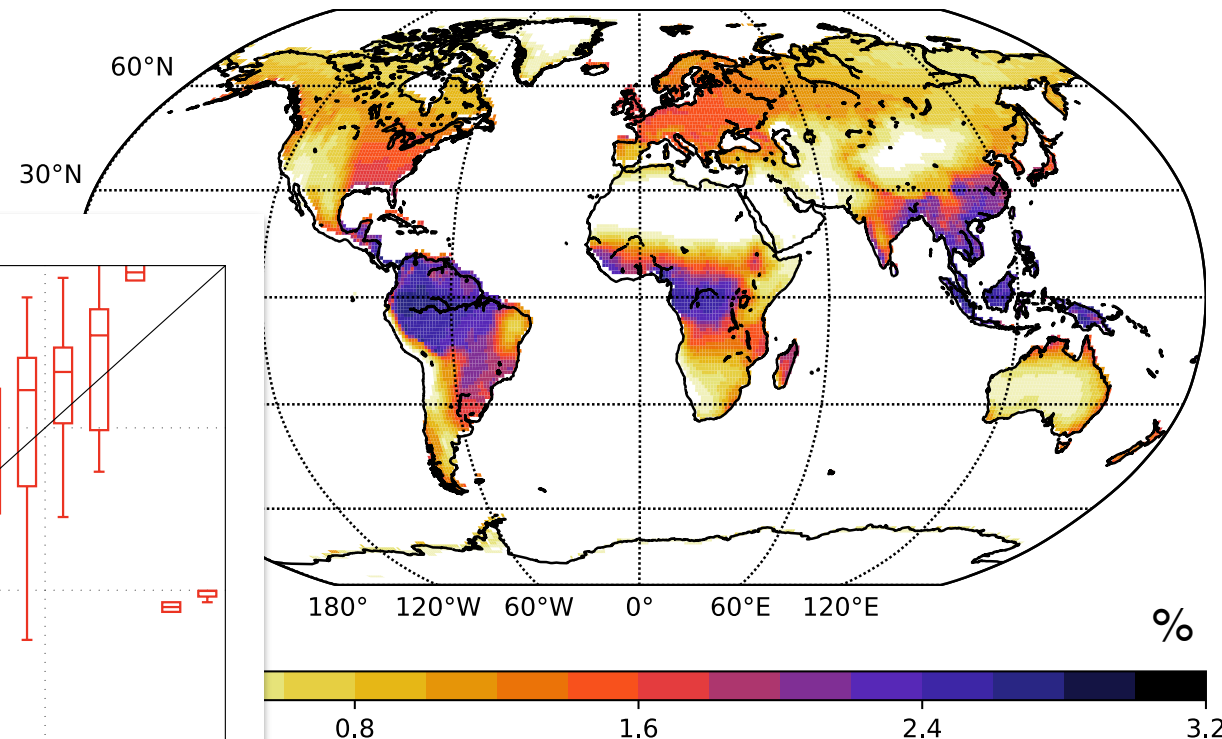
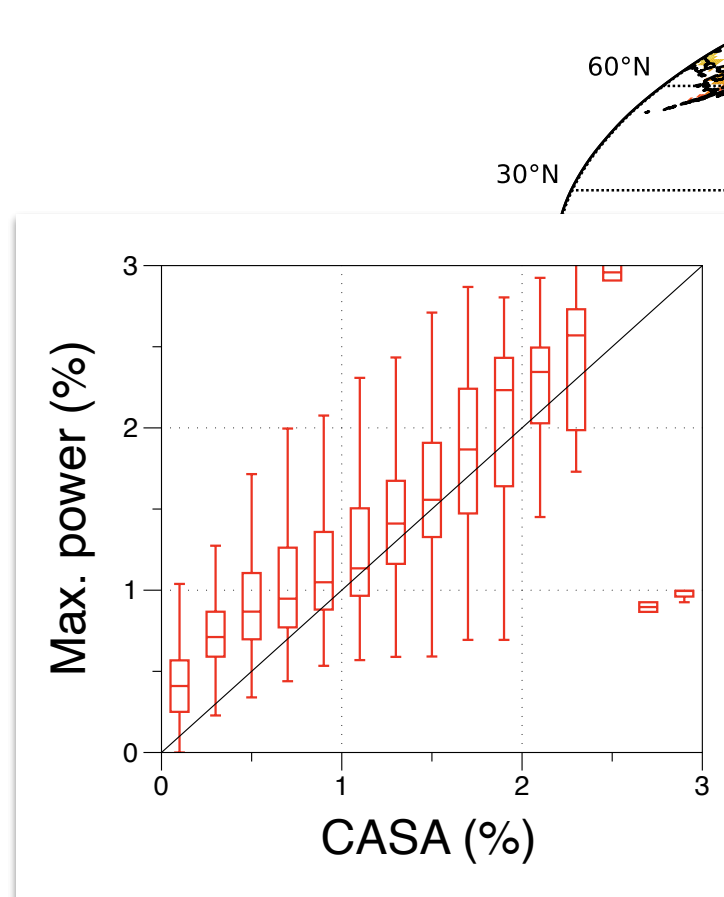


Water use
efficiency:
 $2 \text{ gCO}_2/\text{kg H}_2\text{O}$

$\text{CH}_2\text{O}, \text{O}_2 \rightarrow \text{H}_2\text{O}, \text{CO}_2$



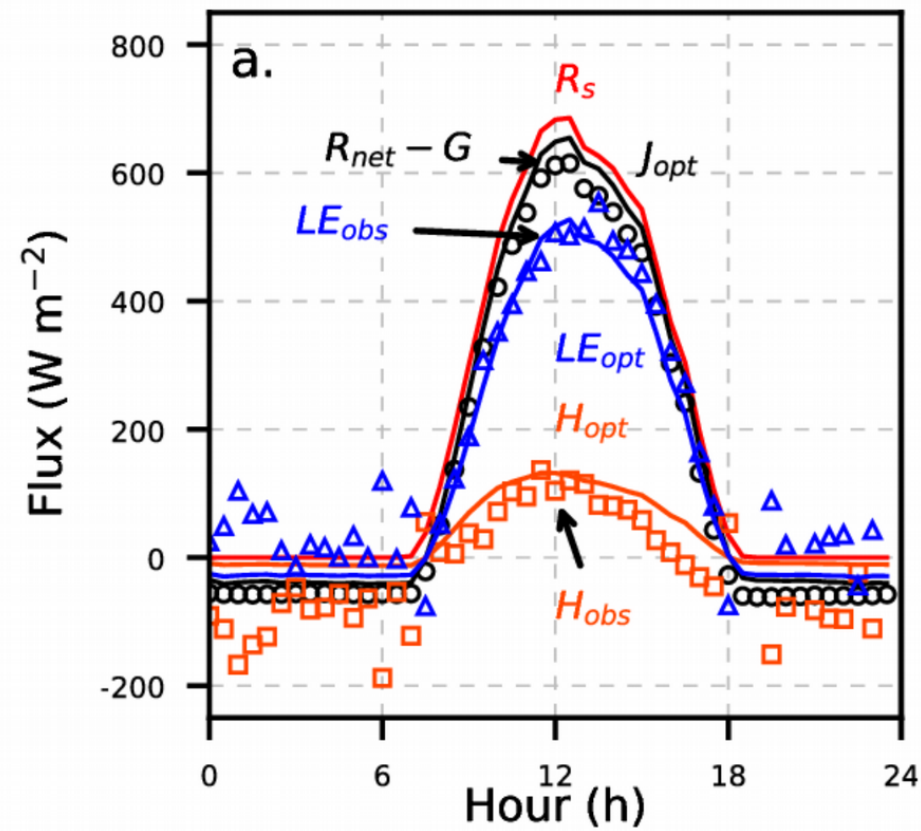
Dissipative
Heating
(high entropy)



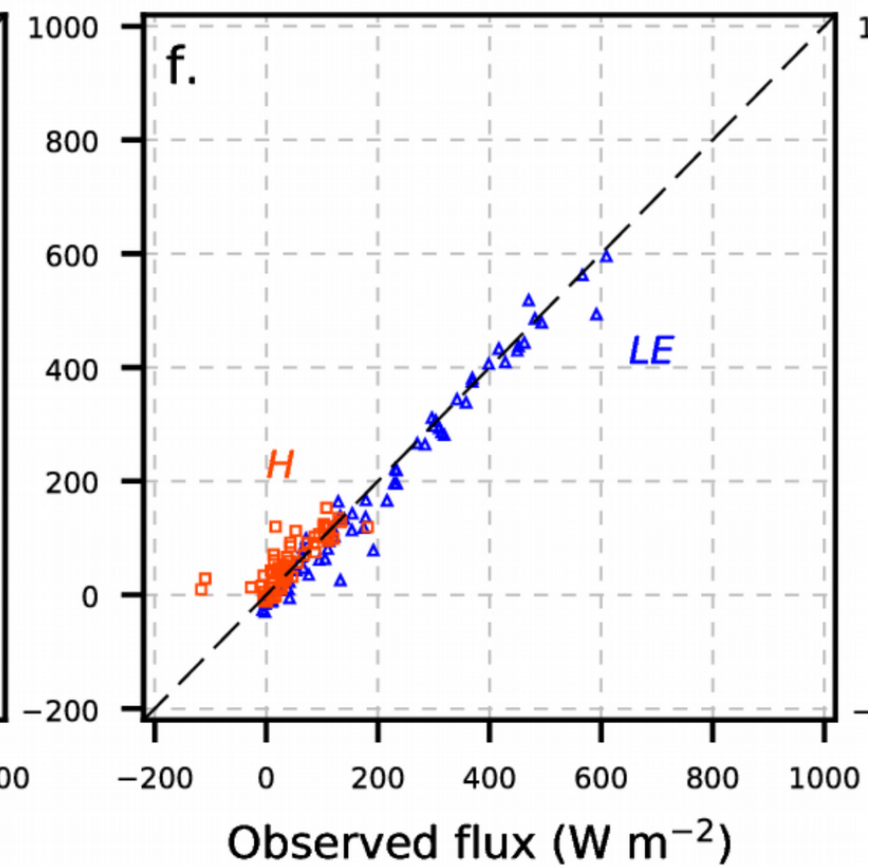
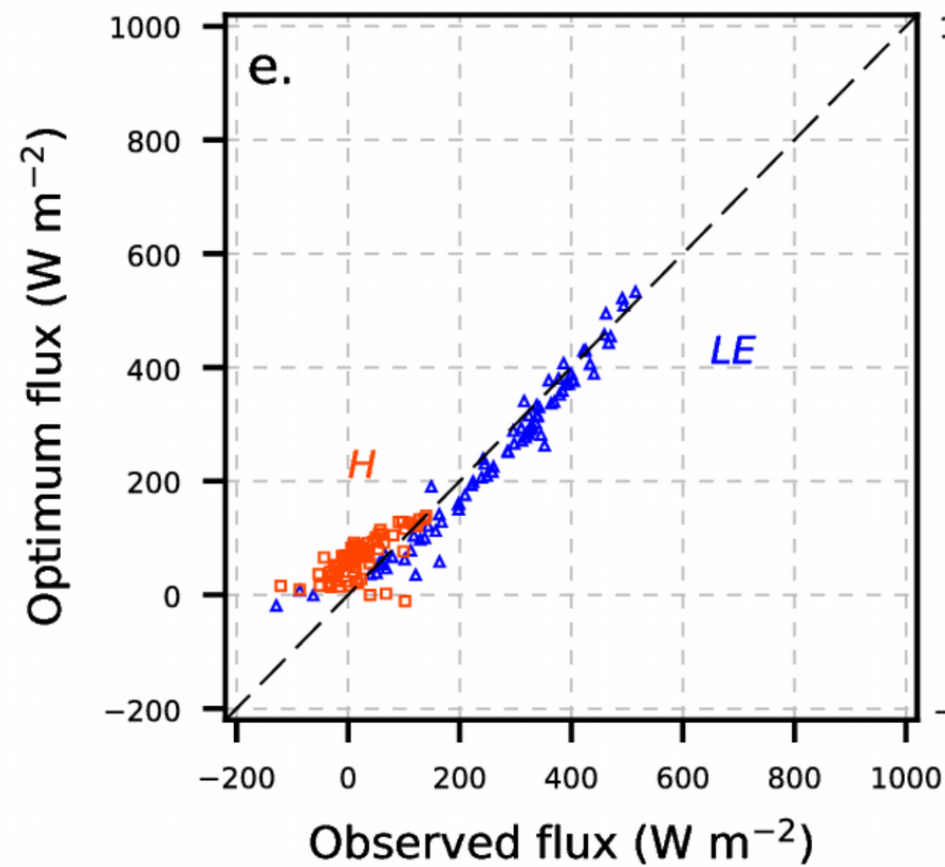
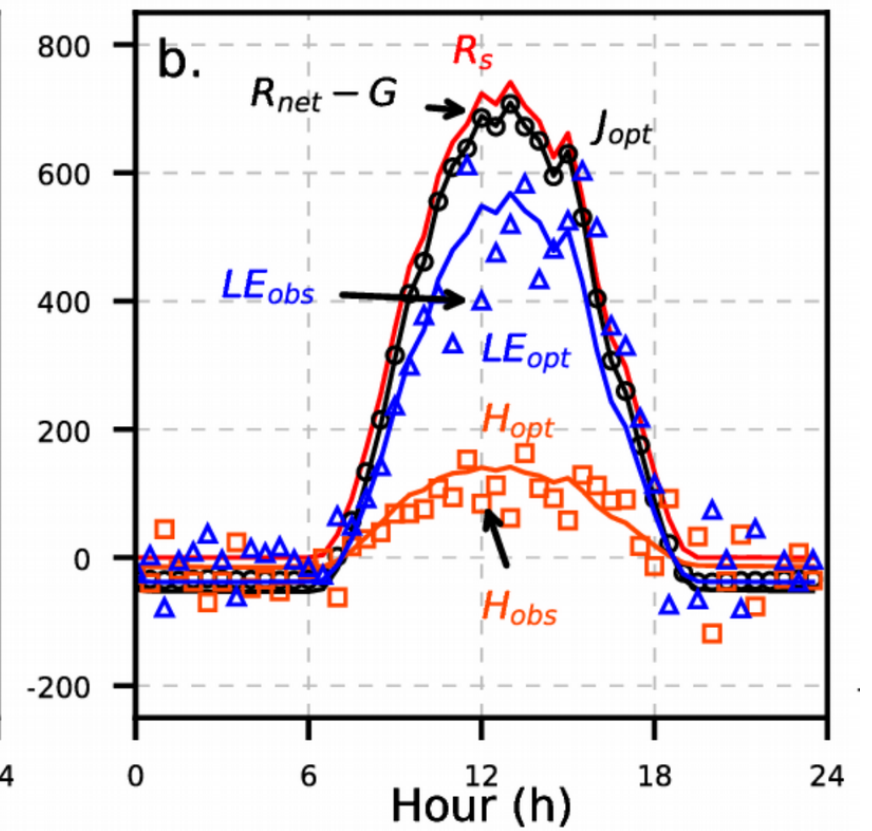
Kleidon (2021) BBA Bioenergetics
Data: NASA-CERES; CASA-GFED



Rain forest, Jun 2016

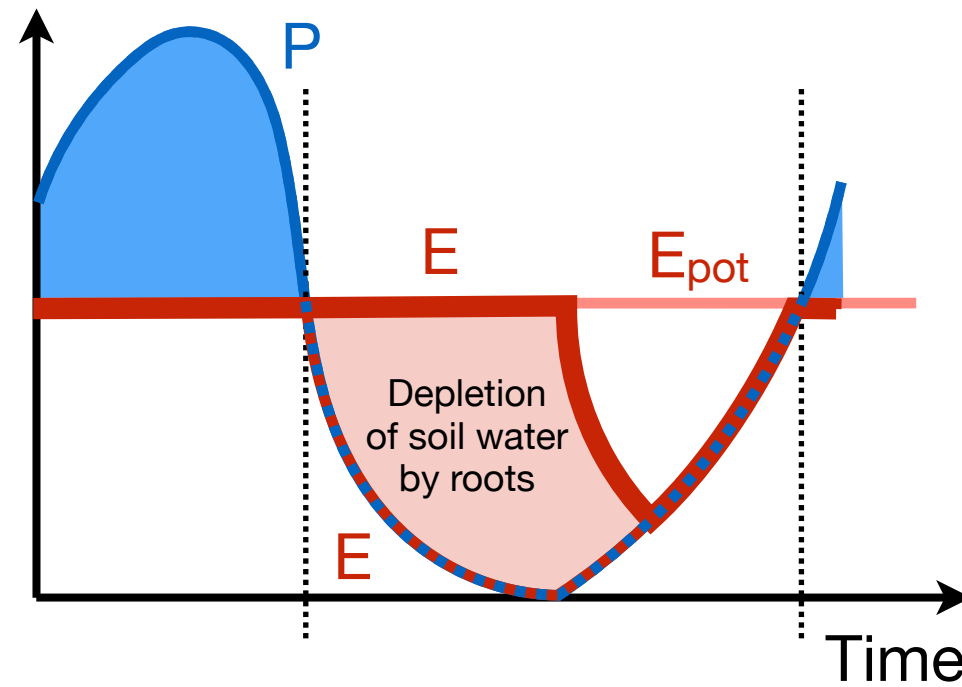


Rain forest, Jan 2017



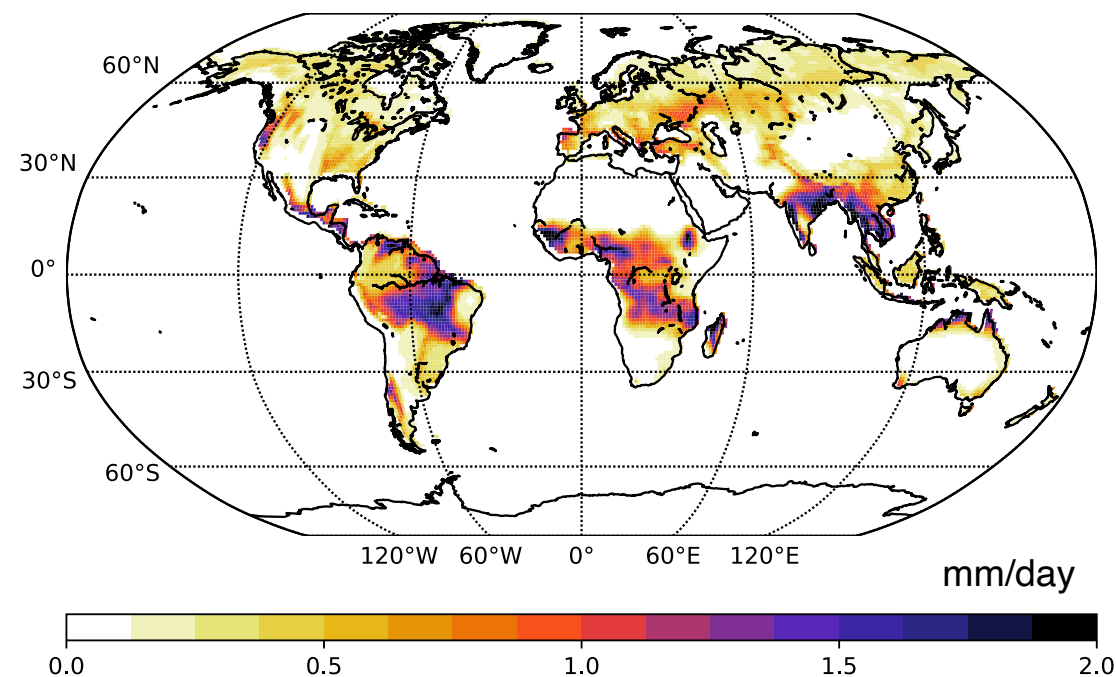


Pushing the Limit



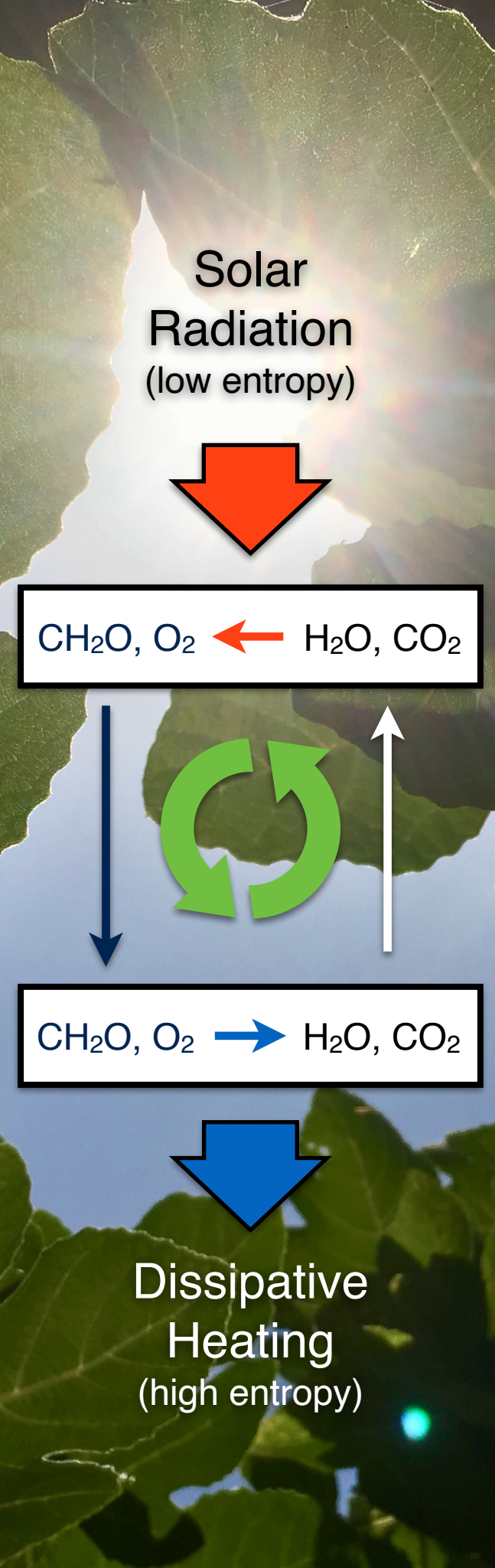
Root systems provide access to soil water storage, reducing the water deficit during dry seasons and enhancing evaporation

Enhancement by rooting zone storage



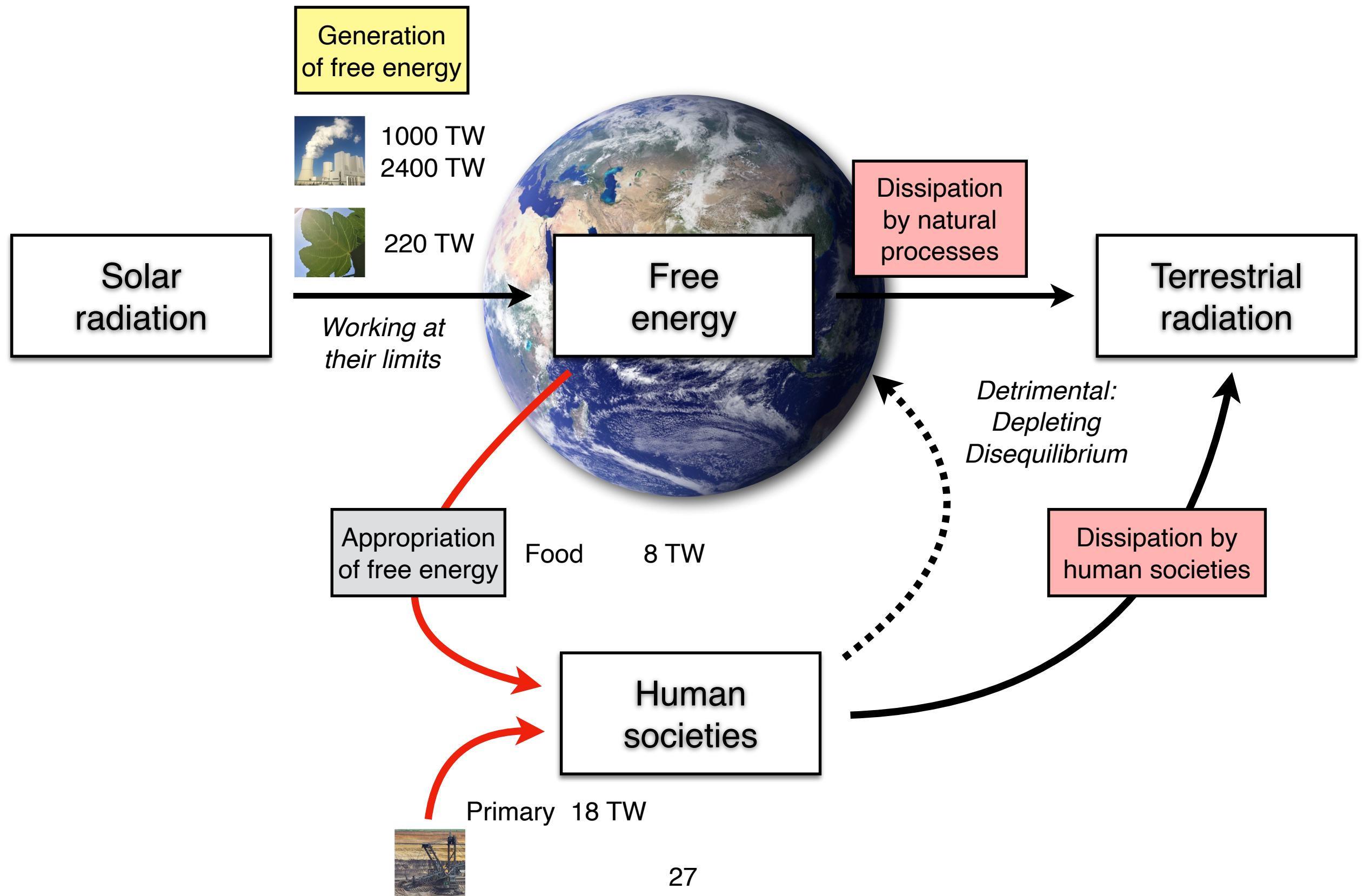
+12%

Powering Life

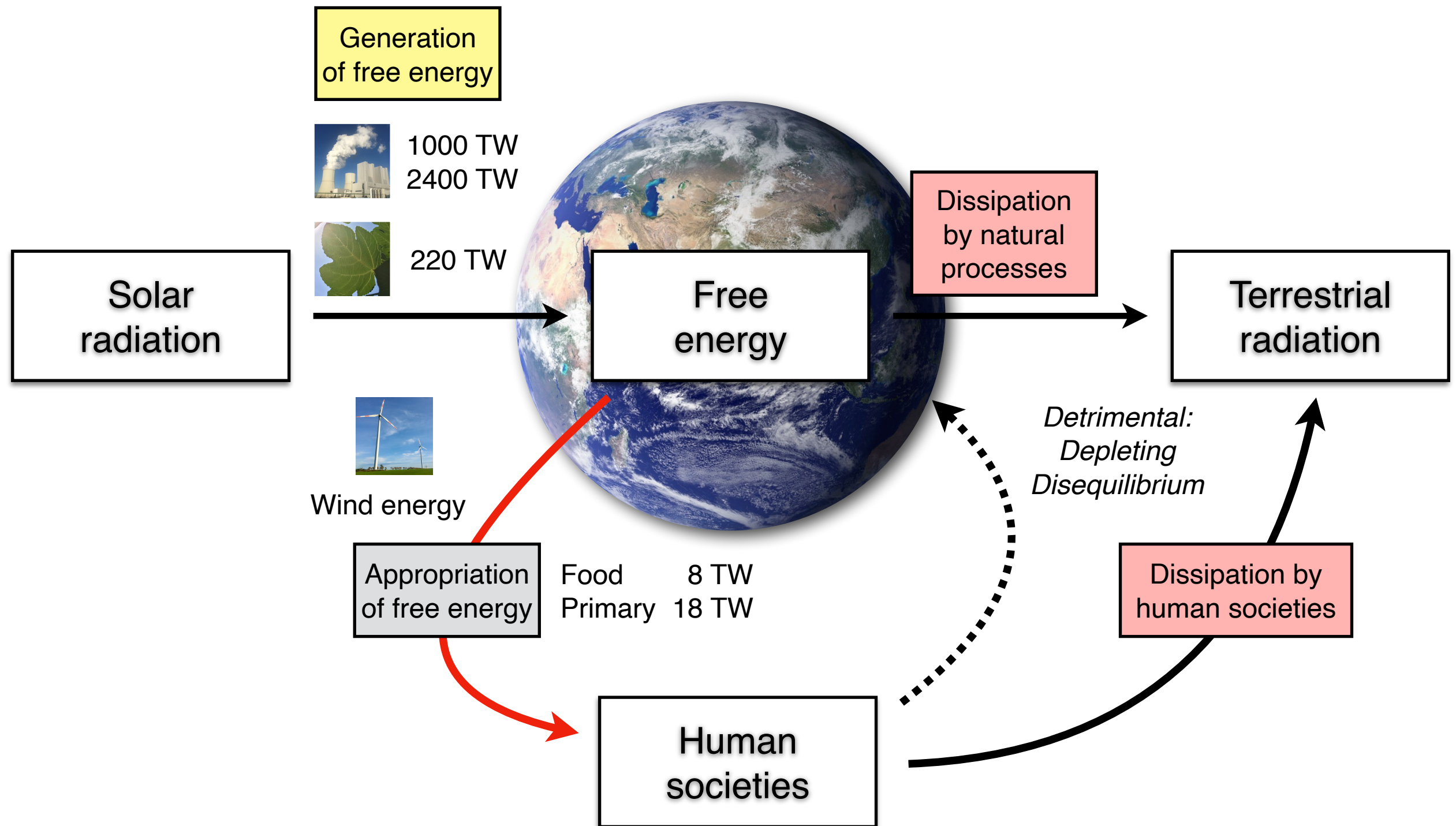


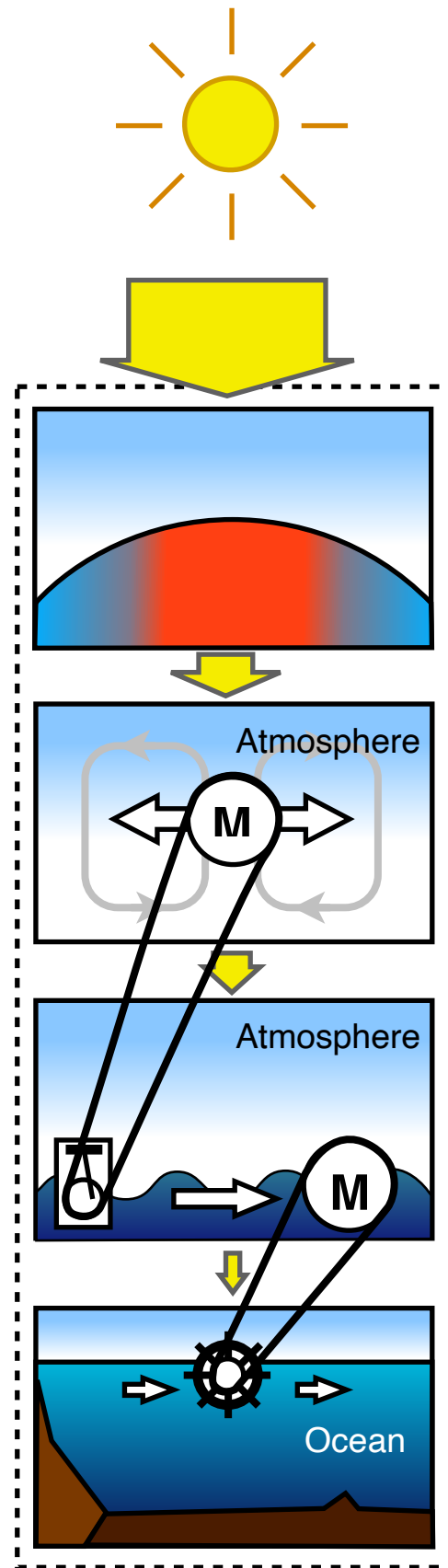
- **Disequilibrium:** Carbohydrates and oxygen
 - Generated by photosynthesis
 - Dissipated by metabolic activities of producers and consumers
- **“Photon” Engine:** Photosynthesis uses sunlight directly to perform work of splitting water and separate charges
- **Working at the limit:** Indirect bottleneck on gas exchange, linked to evaporation
- **Pushing the limit:** Root systems maximize ability to maintain gas exchange during dry episodes
- **Implication:** Biotic activity predictable by gas exchange constraint (radiation, precipitation)

Powering Human Societies



Powering Human Societies





Follow the Energy

Radiation

≈ 175000 TW

→ Solar power



Thermalisation
Differential heating

Thermal energy

≈ 49000 TW



Atmospheric
heat engine

Kinetic energy

≈ 1000 TW

→ Wind power



Ocean energy
input

Wave energy

≈ 65 TW

→ Wave power



Kinetic energy

≈ 5 TW

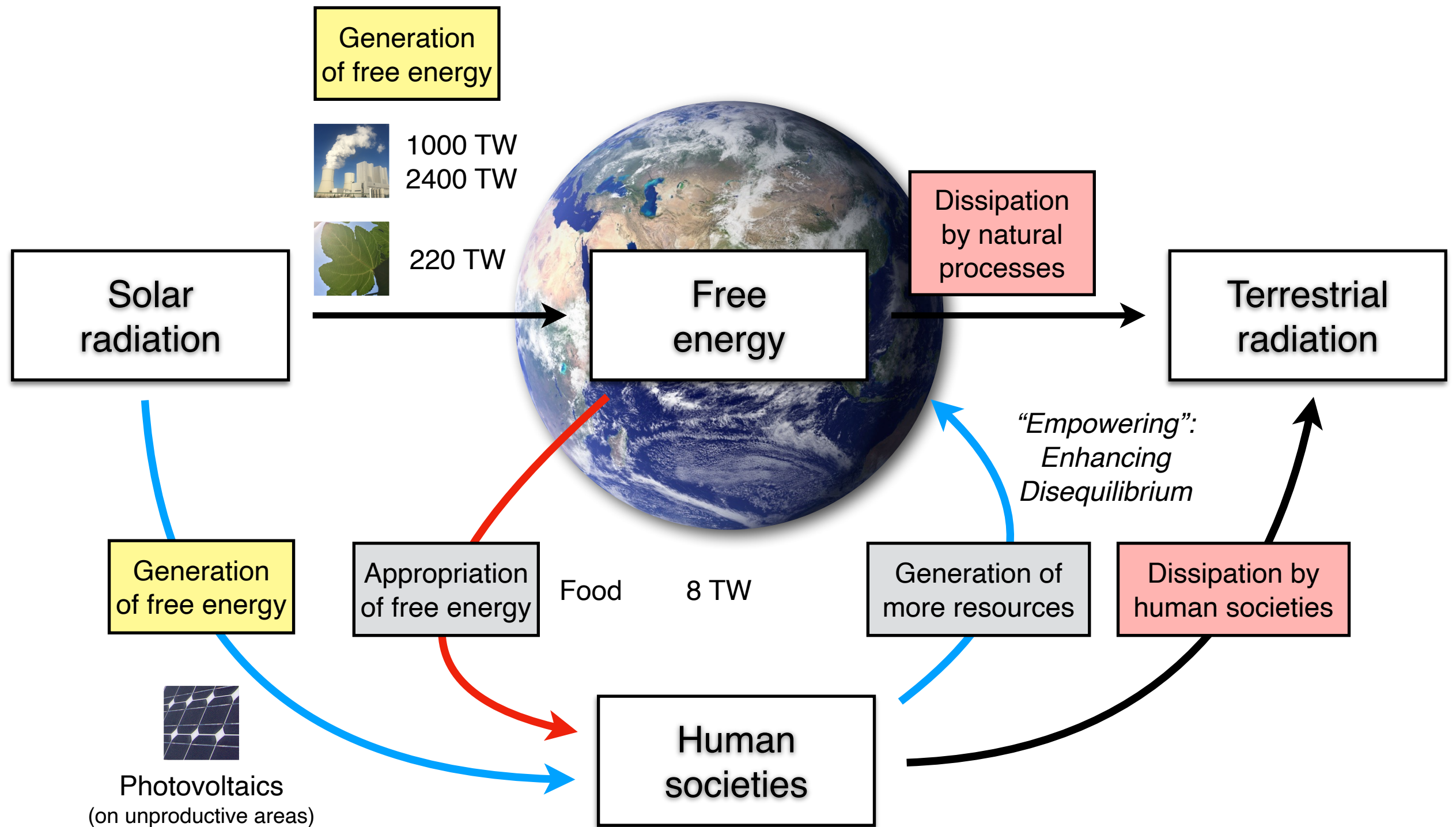
→ Ocean power

Geothermal $\ll 50$ TW

Human energy demand ≈ 18 TW

Tidal ≈ 5 TW

Powering Human Societies





Working at the limit

How thermodynamics shapes the Earth system

- **Entropy** sets fundamental **directions** and **limits**
(beyond heat, includes interactions)
- Constrains the **work** needed to sustain dissipative dynamics
(climate, life, human societies)
- Climate, hydrologic cycling, and biotic productivity at their **limits**
("maximum power", directly or indirectly)
- "**Simplicity**" in complex Earth system and global change
- Detrimental vs. beneficial effects of **human activity**
- **Evolutionary direction** for Earth's past and future?

Working at the limit

How thermodynamics shapes the Earth system



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